Package 'KSD'

January 20, 2025

Type Package

Title Goodness-of-Fit Tests using Kernelized Stein Discrepancy

Version 1.0.1

Date 2021-01-11

Description An adaptation of Kernelized Stein Discrepancy, this package provides a goodness-of-fit test of whether a given i.i.d. sample is drawn from a given distribution. It works for any distribution once its score function (the derivative of log-density) can be provided. This method is based on ``A Kernelized Stein Discrepancy for Goodness-of-fit Tests and Model Evaluation" by Liu, Lee, and Jordan, available at <arXiv:1602.03253>.

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LazyData TRUE

RoxygenNote 7.1.1

Imports pryr, graphics, stats

Suggests datasets, ggplot2, gridExtra, mclust, mvtnorm

NeedsCompilation no

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Repository CRAN

Date/Publication 2021-01-11 08:50:16 UTC

Contents

Index **[11](#)**

---

demo_gmm	*Tests 1-dimensional Gaussian Mixture Models.*

Description

Tests 1-dimensional Gaussian Mixture Models.

Usage

```
demo_gmm()
```

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demo_gmm_multi	*Tests multidimensional Gaussian Mixture Models.*

Description

Tests multidimensional Gaussian Mixture Models.

Usage

```
demo_gmm_multi()
```

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demo_iris	*Fits Gaussian Mixture model and computes the KSD value for the model*

Description

We fit a Gaussian Mixture Model for a given dataset (Fisher's Iris), and we compute the KSD P-value on the hold-out test dataset. User may tune the parameters and observe the change in results. Reports average of p-values obtained during each k-fold. It also plots the contour for each k-fold iteration if only 2 dimensions of data are used. If a vector is specified for nClust, the code tries each element as the number of clusters and reports the optimal parameter by choosing one with highest p-value.

Usage

```
demo_iris(cols = c(1, 2), nClust = 3, kfold = 5)
```

Arguments

cols	: Columns of iris data set to use. If 2 dimensions, plots the contour for each k-fold.
nClust	: Number of clusters want to estimate with If vector, use each element as number of clusters and reports the optimal number.
kfold	: Number of k to use for k-fold

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demo_normal_performance

Shows KSD p value change with respect variation in noise

Description

We generate a standard normal distribution, and add varying gaussian noise to this dataset and see the change in pvalues.

Usage

```
demo_normal_performance()
```

---

demo_simple_gamma *Tests 1-dimensional Gamma Distribution with customized parameters*

Description

We generate a gamma distribution with given parameters, and add gaussian noise to this dataset. We then compute the score of each dataset for the original true distribution.

Usage

```
demo_simple_gamma(
  trueshape = 10,
  truescale = 3,
  noisemu = 5,
  noisesd = 2,
  n = 100
)
```

Arguments

trueshape	shape of true gamma distribution
truescale	scale of true gamma distribution
noisemu	mean of gaussian noise to add
noisesd	standard deviation of gaussian noise to add
n	number of samples to generate

---

demo_simple_gaussian	*Tests 1-dimensional Gaussian Distribution with customized parameters*

Description

We generate a gaussian distribution with given parameters, and add noise to this dataset. We then compute the score of each dataset for the original true distribution.

Usage

```
demo_simple_gaussian(truemu = 5, truesd = 1, noisemu = 0, noisesd = 2, n = 100)
```

Arguments

truemu	mean of true distribution
truesd	standard deviation of true distribution
noisemu	mean of gaussian noise to add
noisesd	standard deviation of gaussian noise to add
n	number of samples to generate

---

gmm	*Returns a Gaussian Mixture Model*

Description

Returns a Gaussian Mixture Model

Usage

```
gmm(nComp = NULL, mu = NULL, sigma = NULL, weights = NULL, d = NULL)
```

Arguments

nComp	(scalar) : number of components
mu	(d by k): mean of each component
sigma	(d by d by k): covariance of each component
weights	(1 by k) : mixing weight of each proportion (optional)
d	: number of dimensions of vector (optional)

Value

model : A Gaussian Mixture Model generated from the given parameters

Examples

```
# Default 1-d gaussian mixture model
model <- gmm()

# 1-d Gaussian mixture model with 3 components
model <- gmm(nComp = 3)

# 3-d Gaussian mixture model with 3 components, with specified mu,sigma and weights
mu <- matrix(c(1,2,3,2,3,4,5,6,7),ncol=3)
sigma <- array(diag(3),c(3,3,3))
model <- gmm(nComp = 3, mu = mu, sigma=sigma, weights = c(0.2,0.4,0.4), d = 3)
```

KSD   *Estimate Kernelized Stein Discrepancy (KSD)*

Description

Estimate kernelized Stein discrepancy (KSD) using U-statistics, and use bootstrap to test H0: x_i is drawn from $p(X)$ (via KSD=0).

Usage

```
KSD(x, score_function, kernel = "rbf", width = -1, nboot = 1000)
```

Arguments

x	Sample of size Num_Instance x Num_Dimension
score_function	($\nabla_x \log p(x)$) Score funtion : takes x as input and output a column vector of size Num_Instance X Dimension. User may use pryr package to pass in a function that only takes in dataset as parameter, or user may also pass in computed score for a given dataset.
kernel	Type of kernel (default = 'rbf')
width	Bandwith of the kernel (when width = -1 or 'median', set it to be the median distance between data points)
nboot	Bootstrap sample size

Value

A list which includes the following variables :

- "ksd" : Estimated Kernelized Stein Discrepancy (KSD)

- "p" : p-Value for rejecting the null hypothesis that ksd = 0

- "bootstrapSamples" : the bootstrap sample

- "info": other information, including : bandwidth, M, nboot, ksd_V

Examples

```
# Pass in a dataset generated by Gaussian distribution,
# use pryr package to pass in score function
model <- gmm()
X <- rgmm(model, n=100)
score_function = pryr::partial(scorefunctiongmm, model=model)
result <- KSD(X,score_function=score_function)

# Pass in a dataset generated by Gaussian distribution,
# pass in computed score rather than score function
model <- gmm()
X <- rgmm(model, n=100)
score_function = scorefunctiongmm(model=model, X=X)
result <- KSD(X,score_function=score_function)

# Pass in a dataset generated by Gaussian distribution,
# pass in computed score rather than score function
# Use median_heuristic by specifying width to be -2.0
model <- gmm()
X <- rgmm(model, n=100)
score_function = pryr::partial(scorefunctiongmm, model=model)
result <- KSD(X,score_function=score_function, 'rbf',-2.0)

# Pass in a dataset generated by specific Gaussian distribution,
# pass in computed score rather than score function
# Use median_heuristic by specifying width to be -2.0
model <- gmm()
X <- rgmm(model, n=100)
score_function = pryr::partial(scorefunctiongmm, model=model)
result <- KSD(X,score_function=score_function, 'rbf',-2.0)
```

---

likelihoodgmm   *Calculates the likelihood for a given dataset for a GMM*

Description

Calculates the likelihood for a given dataset for a GMM

Usage

```
likelihoodgmm(model = NULL, X = NULL)
```

Arguments

model	: The Gaussian Mixture Model
X	(n by d): The dataset of interest, where n is the number of samples and d is the dimension

Value

P (n by k) : The likelihood of each dataset belonging to each of the k component

Examples

```
# compute likelihood for a default 1-d gaussian mixture model
# and dataset generated from it
model <- gmm()
X <- rgmm(model)
p <- likelihoodgmm(model=model, X=X)
```

---

perturbgmm   *Returns a perturbed model of given GMM*

Description

Returns a perturbed model of given GMM

Usage

```
perturbgmm(model = NULL)
```

Arguments

model	: The base Gaussian Mixture Model

Value

perturbedModel : Perturbed model with added noise to the supplied GMM

Examples

```
#Add noise to default 1-d gaussian mixture model
model <- gmm()
noisymodel <- perturbgmm(model)
```

---

plotgmm   *Plots histogram for 1-d GMM given the dataset*

Description

Plots histogram for 1-d GMM given the dataset

Usage

```
plotgmm(data, mu = NULL)
```

Arguments

data   (n by 1): The dataset of interest, where n is the number of samples.

mu   : True mean of the GMM (optional)

Examples

```
# Plot pdf histogram for a given dataset
model <- gmm()
X <- rgmm(model)
plotgmm(data=X)

# Plot pdf histogram for a given dataset, with lines that indicate the mean
model <- gmm()
mu <- model$mu
X <- rgmm(model)
plotgmm(data=X, mu=mu)
```

---

posteriorgmm   *Calculates the posterior probability for a given dataset for a GMM*

Description

Calculates the posterior probability for a given dataset for a GMM

Usage

```
posteriorgmm(model = NULL, X = NULL)
```

Arguments

model   : The Gaussian Mixture Model

X   (n by d): The dataset of interest, where n is the number of samples and d is the
                    dimension

Value

P (n by k) : The posterior probabilty of each dataset belonging to each of the k component

Examples

```
# compute posterior probability for a default 1-d gaussian mixture model
# and dataset generated from it
model <- gmm()
X <- rgmm(model)
p <- posteriorgmm(model=model, X=X)
```

---

rgmm	*Generates dataset from Gaussian Mixture Model*

Description

Generates dataset from Gaussian Mixture Model

Usage

```
rgmm(model = NULL, n = 100)
```

Arguments

model   : Gaussian Mixture Model defined by gmm()

n   : number of samples desired

Value

data (n by d): Random dataset generated from given the Gaussian Mixture Model

Note

Requires library mvtnorm

Examples

```
#Generate 100 samples from default gaussian mixture model
model <- gmm()
X <- rgmm(model)

#Generate 300 samples from 3-d gaussian mixture model
model <- gmm(d=3)
X <- rgmm(model,n=300)
```

---

scorefunctiongmm   *Score function for given GMM : calculates score function dlogp(x)/dx*
                            for a given Gaussian Mixture Model

---

Description

Score function for given GMM : calculates score function dlogp(x)/dx for a given Gaussian Mixture
Model

Usage

```
scorefunctiongmm(model = NULL, X = NULL)
```

Arguments

model   : The Gaussian Mixture Model

X   (n by d): The dataset of interest, where n is the number of samples and d is the
                 dimension

Value

y : The score computed by the given function

Examples

```
# Compute score for a given gaussianmixture model and dataset
model <- gmm()
X <- rgmm(model)
score <- scorefunctiongmm(model=model, X=X)
```

Index